

# MA280 Probability (Online)

| Instructor<br>Information     | Shen Fan Home Institution: China University of Petroleum Email: fans@cup.edu.cn  |         |         |
|-------------------------------|--|---------|---------|
| Term                          | June 27, 2022<br>- July 22, 2022   | Credits | 4 units |
| Course Delivery               | The class will be delivered in the format of online. Other than recorded lecture videos, the instructor will arrange 4 hours' real-time interactions with students per week (via Tencent Meeting and WeChat group). The workload students are expected to complete to properly pass this course is about 10-15 hours per week. |         |         |
| Required Texts<br>(with ISBN) | A First Course in Probability, 10th Edition. S. Ross. Pearson ISBN-13: 9780134753119.  |         |         |
| Prerequisite                  |  | N/A     |         |



### **Course Overview**

This course introduces students to probability. Topics include probability spaces, conditional probability, independence, univariate random variables, multivariate random variables, random vectors, expectation, law of large numbers, central limit theorem.

### **Course Goals**

A student who satisfactorily completes this course will be able to:

- ♦ understand the basic rules of probability, conditional probability and expectation;
- ♦ apply Bayes' theorem on changing conditional probabilities with new evidence;
- ♦ understand the difference between discrete and continuous random variables;
- ♦ work easily with several common distributions, discrete and continuous;
- ♦ know what expectation and variance mean and be able to compute them;
- ♦ understand the central limit theorem.

#### **Exams**

Midterm Exam (30%): 2 hours' Written Test

Final Exam (40%): 2 hours' Written Test



# **Grading Policy**

| Туре                   | Description                      | Weight |
|------------------------|----------------------------------|--------|
| Homework               | Short answer questions           | 30%    |
| Midterm<br>Examination | Written Test; On-line Submission | 30%    |
| Final Exam             | Written Test; On-line Submission | 40%    |

# **Grading Scale**

| Number grade | Letter grade | GPA |
|--------------|--------------|-----|
| 90-100       | A            | 4.0 |
| 85-89        | A-           | 3.7 |
| 80-84        | B+           | 3.3 |
| 75-79        | В            | 3.0 |
| 70-74        | B-           | 2.7 |
| 67-69        | C+           | 2.3 |
| 65-66        | С            | 2.0 |
| 62-64        | C-           | 1.7 |
| 60-61        | D            | 1.0 |
| ≤59          | F (Failure)  | 0   |



### **Class Schedule**

| Date   | Lecture   | Readings  | Online Teaching<br>Arrangement  |
|--------|---|-----------|---|
| Day 1  | Combinatorial Analysis  | Chapter 1 | approximately 80 minutes pre-recorded video lectures  |
| Day 2  | Axioms of probability, sample spaces having equally likely outcomes   | Chapter 2 | approximately 80 minutes<br>pre-recorded video lectures<br>plus 120 minutes online<br>interaction via Tencent<br>Meeting and WeChat group |
| Day 3  | Conditional probability, Bayes formula  | Chapter 3 | approximately 80 minutes pre-recorded video lectures  |
| Day 4  | Independent events, $P(\cdot   F)$ is a Probability   | Chapter 3 | approximately 80 minutes pre-recorded video lectures  |
| Day 5  | Discrete random variables, expectation and variance of discrete random variables,                                     | Chapter 4 | approximately 80 minutes<br>pre-recorded video lectures<br>plus 120 minutes online<br>interaction via Tencent<br>Meeting and WeChat group |
| Day 6  | Some Important Discrete Probability Distributions   | Chapter 4 | approximately 80 minutes pre-recorded video lectures  |
| Day 7  | Continuous random variables,<br>expectation and variance of<br>continuous random variables                            | Chapter 5 | approximately 80 minutes pre-recorded video lectures  |
| Day 8  | Some important continuous probability Distributions, the distribution of a function of a random variable.             | Chapter 5 | approximately 80 minutes<br>pre-recorded video lectures<br>plus 120 minutes online<br>interaction via Tencent<br>Meeting and WeChat group |
| Day 9  | Jointly distributed random variables,<br>joint distribution functions,<br>independent random variables                | Chapter 6 | approximately 80 minutes pre-recorded video lectures  |
| Day 10 | Conditional distributions,<br>order statistics,<br>joint probability distribution of<br>functions of random variables | Chapter 6 | approximately 80 minutes<br>pre-recorded video lectures<br>plus 120 minutes online<br>interaction via Tencent<br>Meeting and WeChat group |
| Day 11 | Midterm   |           | online Midterm Exam   |
| Day 12 | Properties of expectation,<br>expectation and variance of sums of<br>random variables,<br>covariance and correlations | Chapter 7 | approximately 80 minutes pre-recorded video lectures  |
| Day 13 | Conditional expectation, conditional expectation and prediction, moment generating functions                          | Chapter 7 | approximately 80 minutes<br>pre-recorded video lectures<br>plus 120 minutes online<br>interaction via Tencent<br>Meeting and WeChat group |



| Day 14 | Additional properties of normal random variables, general definition of expectation                                  | Chapter 7  | approximately 80 minutes pre-recorded video lectures  |
|--------|--|------------|---|
| Day 15 | Chebyshev's inequality and the weak law of large numbers, the central limit theorem, the strong law of large numbers | Chapter 8  | approximately 80 minutes<br>pre-recorded video lectures<br>plus 120 minutes online<br>interaction via Tencent<br>Meeting and WeChat group |
| Day 16 | Other inequalities and a Poisson limit result  | Chapter 8  | Approximately 80 minutes pre-recorded video lectures  |
| Day 17 | A Brief Introduction to Additional<br>Topics in Probability  | Chapter 9  | approximately 80 minutes<br>pre-recorded video lectures<br>plus 120 minutes online<br>interaction via Tencent<br>Meeting and WeChat group |
| Day 18 | A Brief Introduction to Simulation   | Chapter 10 | approximately 80 minutes pre-recorded video lectures  |
| Day 19 | Final Review   |            | approximately 80 minutes<br>pre-recorded video lectures<br>plus 120 minutes online<br>interaction via Tencent<br>Meeting and WeChat group |
| Day 20 | Final Exam   |            | On-line Submission  |