

## Shanghai Jiao Tong University

# MA413 Time Series & Random Processes in Linear Systems

Instructor Information:	Wanchunzi Yu Home Institution: Bridgewater State University Email: wyu@bridgew.edu Office Hours: Determined by Instructor		
Term:	December 16, 2019 - January 7, 2020	Credits:	4 units
Class Hours:	Monday through Friday, 160 mins per teaching day		
Discussion Sessions:	2 hours each week, conducted by teaching assistant(s)		
Total Contact Hours:	64 contact hours (1 contact hour = 45 mins, 2880 mins in total)		
Required Texts (with ISBN):	Time Series Analysis Univariate and Multivariate Methods, 2 <sup>nd</sup> Edition, by William W.S. Wei ISBN-13: 978-0321322166 ISBN-10: 0321322169		
Prerequisite:	Financial Mathematics related courses are needed before enrolling in this lesson		



#### **Course Overview**

Time Series & Random Process in Linear System is a course designed for students of Financial Mathematics. This is a course of Time Series Theory for the students specializing in the field of Finance and Banking. The course will cover both various of time series models and the application with financial time series data. Interpretation and conclusion of the analysis results of real-life examples are also importation.



#### **Course Goals**

Upon successful completion of this course, students will be conversant with

- main concepts of Time Series theory and methods of analysis
- analysis and modeling of stochastic processes of ARMA models
- seasonal ARIMA models
- autoregressive models
- co-integration and error correction models
- Spectrum analysis
- forecasting using transfer function models
- working with real-life economic time series data using the statistical software

#### **Grading Policy**

Attendance	20%
Assignment 1	15%
Assignment 2	15%
Midterm Exam	25%
Final Exam	25%

#### Grading Scale is as follows

Number grade	Letter grade	GPA
90-100	А	4
85-89	A-	3.7
80-84	B+	3.3
75-79	В	3
70-74	B-	2.7
67-69	C+	2.3
65-66	С	2
62-64	C-	1.7
60-61	D	1
≤59	F (Failure)	0



### **Class Schedule**

Date	Lecture	Chapter
	1.1 Introduction	
	1.2 Examples and Scope of This Book	1, 2
Day 1	2.1 Stochastic Processes	
Day 1	2.2 The Autocovariance and Autocorrelation Functions	
	2.3 The Partial Autocorrelation Function	
	2.4 White Noise Processes	
	2.5 Estimation of the Mean, Autocovariances, and	
	Autocorrelations	2.2
	2.6 Moving Average and Autoregressive Representations of	2, 3
Day 2	Time Series Processes	
	2.7 Linear Difference Equations	
	3.1 Autoregressive Processes	
	3.2 Moving Average Processes	2
	3.3 The Dual Relationship Between AR(p) and MA (q)	3
Day 3	Processes	
	3.4 Autoregressive Moving Average ARMA (p, q)	
	Processes	
	4.1 Nonstationary in the Mean	4
Day 4	4.2 Autoregressive Integrated Moving Average (ARIMA)	
·	Models	
	4.3 Nonstationary in the Variance and the Autocovariance	
	5.1 Introduction	5
Day 5	5.2 Minimum Mean Square Error Forecasts	Ŭ
	5.3 Computation of Forecasts	
	5.4 The ARIMA Forecast as a Weighted Average of Previous	
	Observations	
	5.5 Updating Forecasts	
	5.6 Eventual Forecast Functions	
	6.1 Steps for Model Identification	6
Day 6	6.2 Empirical Examples	
	6.3 The Inverse Autocorrelation Function (IACF)	
	7.1 The Method of Moments	7
Day 7	7.2 Maximum Likelihood Method	
	7.3 Nonlinear Estimation	
	7.4 Ordinary Least Squares (OLS) Estimation in Time Series	
	Analysis	
	7.5 Diagnostic Checking	



8.1 General Concepts	8
-	
8.3 Seasonal ARIMA Models	
11.1 General Concepts	11
11.2 Orthogonal Functions	
11.3 Fourier Representation of Finite Sequences	
11.4 Fourier Representation of Periodic Sequences	
11. 5 Fourier Representation of Nonperiodic Sequences	
11.6 Fourier Representation of Continuous-Time Functions	
11.7 The Fast Fourier Transform	
12.1 The Spectrum	12
12.2 The Spectrum of Some Common Processes	
12.3 The Spectrum of Linear Filters	
12.4 Aliasing	
13.1 Periodogram Analysis	13
13.2 The Sample Spectrum	
13.3 The Smoothed Spectrum	
13.4 ARMA Spectral Estimation	
14.1 Single-Input Transfer Function Models	14
14.2 The Cross-Correlation Function and Transfer Function	
Models	
14.3 Construction of Transfer Function Models	
14.4 Forecasting Using Transfer Function Models	14
14.5 Bivariate Freqency-Domain Analysis	
14.6 The Cross-Spectrum and Transfer Function Models	
14.7 Multiple-Input Transfer Function Models	
Exam 1	
Exam 2	
	8.2 Traditional Methods   8.3 Seasonal ARIMA Models   11.1 General Concepts   11.2 Orthogonal Functions   11.3 Fourier Representation of Finite Sequences   11.4 Fourier Representation of Periodic Sequences   11.5 Fourier Representation of Nonperiodic Sequences   11.6 Fourier Representation of Continuous-Time Functions   11.7 The Fast Fourier Transform   12.1 The Spectrum   12.2 The Spectrum of Some Common Processes   12.3 The Spectrum of Linear Filters   12.4 Aliasing   13.1 Periodogram Analysis   13.2 The Sample Spectrum   13.3 The Smoothed Spectrum   13.4 ARMA Spectral Estimation   14.1 Single-Input Transfer Function Models   14.2 The Cross-Correlation Function and Transfer Function Models   14.3 Construction of Transfer Function Models   14.4 Forecasting Using Transfer Function Models   14.5 Bivariate Freqency-Domain Analysis   14.6 The Cross-Spectrum and Transfer Function Models